## Math 7h <br> Professor: Padraic Bartlett <br> Homework 4: The Art Gallery Problem

Due Tuesday, week 5, at the start of class
UCSB 2014

1. Take a polygon $P$ with $n$ sides. Consider the following task: we want to station observers at the vertices of $P$, such that they can guard the entire "outside" of $P$. In this situation, we assume that the guards cannot "see through" $P$ 's walls, and can only look out from their positions. For example, here is a polygon $P$ being guarded by four guards:


A polygon with observers guarding its outside. Observers are denoted by red vertices; sample sight lines are drawn in pale red.
(a) Suppose that $P$ is an arbitrary polygon with $n$ vertices. What is the maximum number of guards needed to guard the exterior of $P$ ?
(b) Again, suppose that $P$ is an arbitrary polygon with $n$ vertices. What is the minimum number of guards needed to guard the exterior of $P$ ?

