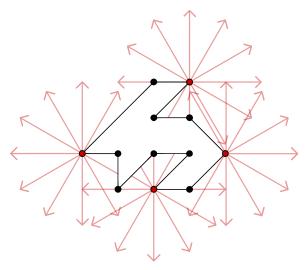
Math 7h

Professor: Padraic Bartlett Homework 4: The Art Gallery Problem

Due Tuesday, week 5, at the start of class UCSB 2014

1. Take a polygon P with n sides. Consider the following task: we want to station observers at the vertices of P, such that they can guard the entire "outside" of P. In this situation, we assume that the guards cannot "see through" P's walls, and can only look out from their positions. For example, here is a polygon P being guarded by four guards:



A polygon with observers guarding its outside. Observers are denoted by red vertices; sample sight lines are drawn in pale red.

- (a) Suppose that P is an arbitrary polygon with n vertices. What is the maximum number of guards needed to guard the exterior of P?
- (b) Again, suppose that P is an arbitrary polygon with n vertices. What is the minimum number of guards needed to guard the exterior of P?