

## Homework 6: Latin Squares and Magic

*Week 3**Mathcamp 2012*

Attempt all of the problems that seem interesting, and let me know if you see any typos! (+) problems are harder than the others. (++) problems are currently open.

1. Construct a magic square of order 5 that does not come from the construction we developed in class.
2. For a  $4 \times 4$  magic square  $M$ , what are the possible values of  $s$  such that the row/column/diagonal sums of  $M$  are  $s$ ?
3. In our lecture, we said that we can construct a pair of orthogonal Latin squares for any  $n$  that is both odd and not a multiple of 3. Does our construction work for any other values of  $n$ ?
4. Even though our construction does not work for even orders, find two mutually orthogonal diagonal Latin squares of order 4 and order 8.
5. Show that there are not two mutually orthogonal diagonal Latin squares of order 6.
6. Despite the above question, find a  $6 \times 6$  magic square.