

7.6 #3

We know that 5 is a primitive root for $p = 1223$ (prime), and that $3^{611} \equiv 1 \pmod{1223}$.

$$5^x \equiv 3 \pmod{1223}$$

and $(p-1)/2 = 611$, so since (a calculator computation shows that mod 1223:
 $3^{10} \equiv 345$, $3^{100} \equiv 729$, $3^{600} \equiv 618$, $3^{611} \equiv 3^{600}3^{10} \equiv 618 * 345 * 3 \equiv 1$)

$$3^{611} \equiv 1 \pmod{1223}, \text{ (rather than } -1)$$

x must be even.